# Two-Dimensional Icosahedral B<sub>12</sub> Networks in Boron-Rich Crystals

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**Abstract.** Two-dimensional icosahedral  $B_{12}$  networks in boron-rich crystals have been examined on the basis of crystal structure data. The linkages between the icosahedral  $B_{12}$  units within the networks are effected approximately along the five-fold axis of  $B_{12}$  icosahedron. Features of the icosahedral  $B_{12}$  networks as well as the external appearances of individual icosahedral  $B_{12}$  units are discussed in connection with the crystal structure-type in which the  $B_{12}$  networks are present. The crystal phases used for the calculations of icosahedral  $B_{12}$  structures are as follows:  $\alpha$ -rhombohedral boron,  $\beta$ -rhombohedral boron,  $\alpha$ -tetragonal boron,  $\alpha$ -AlB<sub>12</sub>,  $\gamma$ -AlB<sub>12</sub>, AlMgB<sub>14</sub>, AlB<sub>24</sub>C<sub>4</sub>, YB<sub>66</sub> and YB<sub>41</sub>Si<sub>12</sub>.

#### 1. Introduction

Boron-rich solids differ from ordinary solids in that it is impossible to interpret their bondings in terms of the conventional rule of valence. As a result, these materials manifest a number of unique properties (such as high-hardness, high-melting points, high-electrical or -thermal conductivity, optical or semi-conducting properties, etc.), which in many cases are of possible technological importance giving rise to a growing interest in their physics and chemistry.

In relation with forms of atomic arrangements, the boron-rich solids are unique in that the boron atoms tend to gather themselves, making up various types of chains and polyhedral units. With increase of the boron content in boride compounds, boron atoms form a pair, a (single, branched, double and triple) zigzag chain, a hexagonal network,  $B_6$  octahedron,  $B_{12}$  cubooctahedron and  $B_{12}$  icosahedron (Fig. 1).

A great many boron-rich crystals principally made up of icosahedral  $B_{12}$  units have so far been synthesized and their structures determined. In the icosahedral  $B_{12}$  crystals, the linkage between  $B_{12}$  icosahedra is almost always performed approximately along their five-fold axes. It is impossible, however, to utilize five-fold rotation symmetry in a twoor three-dimensional periodic network. For that reason the largest boron cluster made up of only the  $B_{12}$  icosahedron is the  $B_{12}(B_{12})_{12}$  unit (Fig. 2), which was discovered in the structure of YB<sub>66</sub> (RICHARD and KASPER, 1969) and is often referred to as a giant icosahedron. Consequently, three dimensional arrangements of  $B_{12}$  icosahedra actually form open although rigid three dimensional frameworks. Except  $\alpha$ -rhomboheral boron



Fig. 1. Variation in bonding nature of boron atoms with increase of the boron content of boride compounds. (a) isolated atoms, (b) pairs, (c) zigzag chain, (d) branched chain, (e) double chain, (f) triple chain, (g) twodimensional network, (h) octahedron, (I) cubooctahedron, (j) icosahedron.



Fig. 2.  $B_{12}(B_{12})_{12}$  giant icosahedron as seen along the two-fold axis.



- Fig. 3. (a)  $B_{28}$  unit as seen along the three-fold rotation-inversion axis, (b)  $B_{20}$ -(C<sub>2</sub>) unit, (c)  $B_{20}$ -(C<sub>s</sub>) unit. The  $B_{20}$ -(C<sub>2</sub>) unit has a vacant apical site at each side of the unit, and the  $B_{20}$ -(C<sub>s</sub>) unit two vacant apical sites at one side.
- Fig. 4. The  $B_{12}$  icosahedron as seen along the (a) two-fold axis, (b) three-fold rotation-inversion axis, (c) fivefold axis.

(DECKER and KASPER, 1959), icosahedral  $B_{12}$  crystals need additional structural entities such as  $B_{28}$  (HOARD *et al.*, 1970),  $B_{22}$  (VLASSE *et al.*, 1979) and  $B_{20}$  units (HIGASHI *et al.*, 1977; HUGHES *et al.*, 1977; HIGASHI, 1983) and isolated boron atoms to fill openings within the three dimensional  $B_{12}$  frameworks. The boron units  $B_{28}$ ,  $B_{22}$  and  $B_{20}$  are condensed icosahedra made up of 3, 2, and 2 icosahedra, respectively (Fig. 3).

In this paper we describe two-dimensional icosahedral  $B_{12}$  networks which extend parallel to or laying on typical crystallographic planes of boron-rich crystals. The icosahedral  $B_{12}$  structures of following materials have been examined. (1)  $\alpha$ -rhombohedral boron and  $B_{6O}$  ( $\alpha$ -rhombohedral boron-type), (2)  $\beta$ -rhombohedral boron ( $\beta$ -rhombohedral borontype), (3)  $\alpha$ -tetragonal boron ( $\alpha$ -tetragonal boron-type), (4)  $\alpha$ -AlB<sub>12</sub> ( $\beta$ -tetragonal borontype) and  $\gamma$ -AlB<sub>12</sub> ( $\gamma$ -AlB<sub>12</sub>-type or related compound of  $\alpha$ -AlB<sub>12</sub>), (5) AlMgB<sub>14</sub> (AlMgB<sub>14</sub>type), (6) AlB<sub>24</sub>C<sub>4</sub> (AlB<sub>24</sub>C<sub>4</sub>-type), (7) YB<sub>66</sub> (YB<sub>66</sub>-type) and YB<sub>41</sub>Si<sub>1.2</sub> (related compound of YB<sub>66</sub>). For reference or comparison with the figures in the text, the B<sub>12</sub> icosahedron is projected in Fig. 4 along its two-fold, three-fold (rotation-inversion), and five-fold axes.

#### 2. Icosahedral $B_{12}$ Networks in the $\alpha$ -Rhomnohedral Boron Structure

The crystal structure of  $\alpha$ -rhombohedral boron (Space group: R  $\overline{3}$  m; a = 0.5057 nm,  $\alpha = 58.07^{\circ}$ ) is shown in Fig. 5, in which each circle centered at the corner of the rhombohedral unit cell stands for the B<sub>12</sub> icosahedron. Linkages between the icosahedra are effected along the five-fold axis in the direction of the crystallographic main axes. There appear three icosahedral  $B_{12}$  networks every periodic translation along the [111] axis. They are all crystallographically equivalent, extending parallel to the (111) plane. In Fig. 6, the icosahedral  $B_{12}$  network as seen along the [111] axis is presented, where every boron atom is depicted with a small circle. The linkages between B<sub>12</sub> icosahedra within each network are performed by the three-centered bond which is indicated (in Fig. 6) with the thin lines connecting adjacent apical B atoms. On the other hand, linkages between icosahedral  $B_{12}$ networks, each of which appears every 1/3 periodic translation along the [111] axis, are made by two-centered bond along the five-fold axes of icosahedra in the direction of the crystallographic main axes (Fig. 5). Two kinds of linkages (two-centered and threecentered bonds) are seen on the icosahedral  $B_{12}$  network on the {100} planes of the rhombohedral structure (Fig. 7). The two-centered-bond is effected along the five-fold axis of the  $B_{12}$  icosahedron in the <100> directions, and the three centered bond is formed in the <110> directions; the latter is presented (in Fig. 7) with a thinner line lying perpendicularly to the [111] direction.

In the structure of  $B_{12}O_2$  ( $\alpha$ -rhombohedral boron structure-type, a = 0.5150 nm,  $\alpha = 62.95^{\circ}$ ), two oxygen atoms are located on the [111] axis in such a way that each of which is enclosed with three  $B_{12}$  icosahedra (Fig. 8) (BORMGREN *et al.*, 1990; HIGASHI *et al.*, 1990). Owing to the incorporation of oxygen atoms, the rhombohedral unit cell volume is increased slightly with a variation of the angle  $\alpha$  from 58.07° to 62.95°. Figure 9 shows the icosahedral  $B_{12}$  network as seen along the [111] axis, which is almost the same as that in  $\alpha$ -rhombohedral boron except the presence of oxygen atoms; each oxygen atom is located at the center of a triangle formed with three  $B_{12}$  icosahedra. The icosahedral  $B_{12}$  network on the {100} plane in this compound is almost the same as that in  $\alpha$ -rhombohedral boron (Fig. 7).



Fig. 5.

Fig. 6.



Fig. 7.

Fig. 5. Structure of  $\alpha$ -rhombohedral boron (space group: R  $\overline{3}$  m; a = 0.5057 nm,  $\alpha = 58.07^{\circ}$ ). Each circle at the lattice point stands for the B<sub>12</sub> icosahedron.

Fig. 6. Icosahedral  $B_{12}$  network in the  $\alpha$ -rhombohedral boron structure as seen along the [111] axis.

Fig. 7. Icosahedral  $B_{12}$  network in the  $\alpha$ -rhombohedral boron structure extending on the {100} planes.



Fig. 8. Structure of  $B_6O$  ( $\alpha$ -rhombohedral boron structure-type, a = 0.5150 nm,  $\alpha = 62.9^\circ$ ). Each circle at the lattice point stands for the  $B_{12}$  icosahedron and smaller ones on the [111] axis oxygen atoms.

Fig. 9. Icosahedral  $B_{12}$  network in the structure of  $B_6O$  as seen along the [111] axis. the smaller circles stand for the oxygen atom.

### 3. Icosahedral $B_{12}$ Networks in $\beta$ -Rhombohedral Boron

Figure 10 shows the crystal structure of  $\beta$ -rhombohedral boron (Space group: R 3 m; a = 1.0145 nm,  $\alpha = 65.17^{\circ}$ ) (HOARD *et al.*, 1970), in which B<sub>12</sub> icosahedra are centered at the corner of the rhombohedral unit cell and the midpoint of the unit cell edges. The largest circles situated on the [111] axis of the unit cell stands for the  $B_{28}$  unit (Fig. 3) and the smallest one at the center of the unit cell an isolated boron atom. With the incorporation of the  $B_{28}$  unit into the rhombohedral unit cell, the angle  $\alpha$  (=65.17°) becomes significantly larger compared to that of  $\alpha$ -rhombohedral boron ( $\alpha = 58.07^{\circ}$ ). There are two kinds of icosahedral networks extending parallel to the (111) plane of the crystal. One appears at the periodic translation of 0, 2/6, and 4/6 along the [111] axis (Fig. 11), and the other at the translation of 1/6, 3/6 and 5/6 along the same axis (Fig. 12). The former is made up of both B<sub>12</sub> and B<sub>28</sub> units and the latter solely of B<sub>12</sub> icosahedra. In Fig. 11, the B<sub>12</sub> and B<sub>28</sub> units are displaying their well-formed appearances which are precisely projected along their respective threefold rotation-inversion axis. On the other hand, in Fig. 12 the  $B_{12}$  icosahedra are arranged with their one of the two-fold axes nearly perpendicularly to the projection plane, thus forming a 3636 kagomé net (PEASON, 1972) as will be seen in some other structure types described in this paper. Another important icosahedral  $B_{12}$  network is that which extends on the  $\{100\}$  plane (Fig. 13). In this network, every  $B_{12}$  icosahedron is situated so as to have its one of the mirror planes just on the (100) plane, forming linear linkages with adjacent icosahedra almost precisely along the five-fold axes. Considering the periodic nature of the crystal structure, the icosahedral B<sub>12</sub> network on the (100) plane should be a 3636 kagomé net.



Fig. 10.

Fig. 11.



Fig. 12.

- Fig. 10. Structure of  $\alpha$ -rhombohedral boron (space group: R  $\overline{3}$  m; a = 1.0145 nm,  $\alpha = 65.17^{\circ}$ ). Each circle at the lattice point and the midpoints of the unit cell edges stands for the B<sub>12</sub> icosahedron. The largest circles on the [111] axis stand for the B<sub>28</sub> unit and the smallest one at the unit cell center an isolated boron atom.
- Fig. 11. Icosahedral  $B_{12}$  network in the  $\beta$ -rhombohedral boron structure as seen along the [111] axis. This network is consisting of the  $B_{12}$  icosahedron and the  $B_{28}$  unit (condensed icosahedra), and appears every periodic translation of 0, 1/3 and 2/3 along the [111] axis. The rhombus drawn in the figure indicates the hexagonal unit plane (001)<sub>hex</sub>.
- Fig. 12. Icosahedral  $B_{12}$  network in the  $\beta$ -rhombohedral boron structure as seen along the [111] axis. It appears every periodic translation of 1/6, 3/6 and 5/6 along the [111] axis.



Fig. 13. Icosahedral  $B_{12}$  network in the  $\beta$ -rhombohedral boron structure extending on the {100} planes.

### 4. Icosahedral $B_{12}$ Network in $\alpha$ -Tetragonal Boron

Figure 14 shows the crystal structure of  $\alpha$ -tetragonal boron (Space group: P4<sub>2</sub>/nm; a = 0.875 nm, c = 0.506 nm) (HOARD *et al.*, 1958). There are four B<sub>12</sub> icosahedra per unit cell, centering the positions: 0.25, 0.25, 0.75; 0.75, 0.25; 0.25, 0.75, 0.25; 0.75, 0.75, 0.75. They coordinate tetrahedrally about an isolated boron atom. The icosahedral B<sub>12</sub> network extending parallel to the (100) plane is presented in Fig. 15. There are two kinds of icosahedral B<sub>12</sub> chains; one is those running along the <100> directions and the other those running along the <101> directions. The linkages between B<sub>12</sub> icosahedra in the former are effected almost along the five-fold axis, on the other hand, those in the latter deviate approximately 20° from the five-fold axis (Fig. 16). It has been reported that the accurate chemical composition of this crystal phase is B<sub>50</sub>C<sub>2</sub> or B<sub>50</sub>N<sub>2</sub>, and the isolated boron atoms should be replaced with either carbon or nitrogen atoms (WILL and KOSSOBUTZKI, 1976). The icosahedral networks in B<sub>50</sub>C<sub>2</sub> or B<sub>50</sub>N<sub>2</sub> are, however, exactly the same as those in  $\alpha$ -tetragonal boron which had previously been reported (HOARD *et al.*, 1958).



Fig. 14.



Fig. 15.

Fig. 16.

Fig. 14. Structure of  $\alpha$ -tetragonal boron as seen along the *c* axis (space group: P4<sub>2</sub>/nnm; *a* = 0.875 nm, *c* = 0.506 nm). The larger cycles stands for the B<sub>12</sub> icosahedron and the smaller one for an isolated boron atom. Each of the isolated boron atoms is tetrahedrally coordinated with four B<sub>12</sub> icosahedra.

Fig. 15. Icosahedral  $B_{12}$  network in the  $\alpha$ -tetragonal boron structure extending parallel to the {100} planes.

Fig. 16. Icosahedral  $B_{12}$  chain in the  $\alpha$ -tetragonal boron structure running along the <101> direction. It shows a significant deviation of  $B_{12}$ - $B_{12}$  linkage from the five-fold axis of the  $B_{12}$  icosahedron.

5. Icosahedral B<sub>12</sub> Networks in the Structure of  $\alpha$ -AlB<sub>12</sub> ( $\beta$ -Tetragonal Boron-Type) and  $\gamma$ -AlB<sub>12</sub> ( $\gamma$ -AlB<sub>12</sub>-Type or Related Compound of  $\alpha$ -AlB<sub>12</sub>)

The structure of  $\alpha$ -AlB<sub>12</sub> is constituted with the B<sub>12</sub> icosahedron and one of the two sorts of B<sub>20</sub> units (HIGASHI et al., 1977; KASPER et al., 1977; HIGASHI, 1983). Full structure of three-dimensional icosahedral  $B_{12}$  framework is presented in Fig. 17. The  $B_{20}$  ( $B_{20}$ -( $C_2$ ) in Fig. 3) unit is accommodated in a large opening of the icosahedral B<sub>12</sub> framework. The Al atoms are situated within relatively small openings outside the B<sub>12</sub> or B<sub>20</sub> units. The structure belongs to the tetragonal system (space group  $P4_12_12$  or  $P4_32_12$ ) with the lattice constants a = 1.017 nm and c = 1.428 nm, and is isostructural with  $\beta$ -tetragonal boron



Fig. 17.

Fig. 18.

- Fig. 17. Structure of  $\alpha$ -AlB<sub>12</sub> (tetragonal, space group: P4<sub>1</sub>2<sub>1</sub>2 or P4<sub>3</sub>2<sub>1</sub>2; a = 1.017 nm and c = 1.428 nm). Each circle stands for the B<sub>12</sub> icosahedron. This type of structure has four-fold and two-fold screw axes (see the text).
- Fig. 18. Icosahedral  $B_{12}$  network in the  $\alpha$ -AlB<sub>12</sub> structure extending parallel to the {101} planes. As to the three sections of the unit plane, an explanation is made in the text.

(VLASSE *et al.*, 1979). It has  $4_1$  or  $4_3$  screw axes in the *c* axes direction at the positions of (0.1/2, z) and (0, 1/2, z), and  $2_1$  screw axes in the <110> directions at z = 0 or 1/2. In the  $\alpha$ -AlB<sub>12</sub> structure, two dimensional icosahedral B<sub>12</sub> networks are observed only parallel with the {101} planes (Fig. 18). All the  $B_{12}$  icosahedra in this structure are crystallographically equivalent. Almost the same icosahedral  $B_{12}$  network as in the  $\alpha$ -AlB<sub>12</sub> structure is present in the  $\gamma$ -AlB<sub>12</sub> structure (Orthorhombic, space group: P2<sub>1</sub>2<sub>1</sub>2<sub>1</sub>; a = 1.657 nm, b = 1.751 nm, c = 1.014 nm) in parallel to the (100) plane. The icosahedral B<sub>12</sub> network in this structure is shown in Fig. 19 in a larger scale than that of Fig. 18. Unlike the  $\alpha$ -AlB<sub>12</sub> structure, three B<sub>12</sub> icosahedra forming a triangle are crystallographically independent from each other, and two sorts of  $B_{20}$  units  $\{B_{20}$ - $(C_2)$  and  $B_{20}$ - $(C_s)\}$  (Fig. 3) are accommodated within openings of the icosahedral B<sub>12</sub> framework (HUGHES et al., 1977; HIGASHI, 1983). In Fig. 20, the relationship of the unit cells and the structures of  $\alpha$ -AlB<sub>12</sub> and  $\gamma$ -AlB<sub>12</sub> in the syntactically intergrown crystal of both phases is given (HIGASHI, 2000). The division of the (101) unit plane in Fig. 18 into three equal parts indicates that equivalent positions of adjacent networks are shifted in the [101] direction by one-third the periodic distance.



Fig. 19. Icosahedral  $B_{12}$  network in the  $\gamma$ -Al $B_{12}$  structure extending parallel to the (100) plane. Fig. 20. Relationship of the unit cells and the structures of  $\alpha$ -Al $B_{12}$  and  $\gamma$ -Al $B_{12}$ .

# 6. Icosahedral B<sub>12</sub> Networks in the AlMgB<sub>14</sub> Structure

The AlMgB<sub>14</sub> compound belongs to the orthorhombic system (space group: Imam) with the lattice constants a = 0.5848 nm, b = 0.8112 nm, c = 1.0312 nm (MATKOVICH and ECONOMY, 1970; HIGASHI and ITO, 1983). Its structure (Fig. 21) is made up of four  $B_{12}$ icosahedra and eight isolated boron atoms per unit cell. The icosahedra are centered at the positions 0,0,0; 1/2,1/2,0; 0,0,1/2 and 1/2,1/2,1/2. Each icosahedron directly links to six icosahedra (first neighbors) approximately along the five-fold axes and to six icosahedra (second neighbors) via isolated boron atoms. The Al and Mg atoms are accommodated within openings outside the icosahedral B<sub>12</sub> framework. The B<sub>12</sub> icosahedra are oriented so as to have one of their mirror planes just on the structural mirror planes situated at the levels of x = 0 and 1/2. Two kinds of icosahedral B<sub>12</sub> networks extending parallel to the (001) plane and (110) planes are shown in Figs. 22 and 23, respectively. In Fig. 22, every icosahedron is oriented so that one of its five-fold axes is approximately perpendicular to the (001) plane. A deviation of B<sub>12</sub>-B<sub>12</sub> bond from the five-fold axes can been seen from the icosahedral B<sub>12</sub> chains running along the [110] direction (Fig. 23). Such a large deviation is unusual except for that in the  $\alpha$ -tetragonal boron structure (Fig. 16). In Fig. 24, a feature of the deviation (about  $17^{\circ}$ ) of  $B_{12}$ - $B_{12}$  bond from the five-fold axis is demonstrated with the icosahedral  $B_{12}$  chain running in the [110] direction.



Fig. 21. Structure of AlMgB<sub>14</sub> as seen along the *a* axis (orthorhombic, space group: Imam; a = 0.5848 nm, b = 0.8112 nm, c = 1.0312 nm). Small circles stand for Mg (dark) and Al (gray) atoms. The less dark circles linking to the icosahedral apical atoms are isolated boron atoms.



Fig. 22.



Fig. 23.

Fig. 24.

- Fig. 22. Icosahedral  $B_{12}$  network in the AlMg $B_{14}$  structure extending parallel to the (001) plane.
- Fig. 23. Icosahedral  $B_{12}^{12}$  network in the AlMg $B_{14}^{14}$  structure extending parallel to the {110} planes. Fig. 24. Icosahedral  $B_{12}$  chain in the AlMg $B_{14}$  structure, showing a deviation of  $B_{12}$ - $B_{12}$  linkage from the fivefold axis of the icosahedron.

# 7. Icosahedral $B_{12}$ Networks in the AlB<sub>24</sub>C<sub>4</sub> Structure

The AlB<sub>24</sub>C<sub>4</sub> compound belongs to the orthorhombic system (space group, Cmam) with the lattice constants a = 0.5690 nm, b = 0.881 nm, c = 0.9100 nm. The structure consists of the  $B_{12}$  icosahedron, containing carbon and isolated boron atoms as essential structural entities (WILL, 1969; PERROTTA et al., 1969). Aluminum atoms are distributed statistically among interstices outside  $B_{12}$  icosahedra. The full structure of the icosahedral  $B_{12}$ framework is presented in Fig. 25. There are two kinds of icosahedral B<sub>12</sub> zigzag chains running in the [001] direction. They are linked to neighboring chains directly through the icosahedral B<sub>12</sub>-B<sub>12</sub> bond along the five-fold axis and indirectly via intermediary carbon atoms. The carbon atoms form C-B-C chains with an isolated boron atom. Each carbon atom in the chain linked to two icosahedral B<sub>12</sub> units, contributing to the construction of the three-dimensional icosahedral B<sub>12</sub> framework. The structure of AlB<sub>24</sub>C<sub>4</sub> can be regarded as a pile in the a axis direction of wavy (or puckered) networks of icosahedral B<sub>12</sub> units; the wave-length and the wave-height correspond to the b axis length and one-half of the *a* axis length, respectively. The plane network of icosahedral  $B_{12}$  units is extending parallel to the (001) plane (Fig. 26), in which the linkage of the  $B_{12}$  icosahedron with the second neighbor B<sub>12</sub> icosahedra are made through intermediary carbon atoms.



Fig. 25. Structure of  $AlB_{24}C_4$  as seen along the *a* axis (orthorhombic, space group: Cmam; a = 0.5690 nm, b = 0.881 nm, c = 0.9100 nm). It corresponds to the projection of a puckered network of icosahedral  $B_{12}$  units (see the text).



Fig. 26. Icosahedral  $B_{12}$  network in the AlB<sub>24</sub>C<sub>4</sub> structure extending parallel to the (001) plane.

### 8. Icosahedral $B_{12}$ Networks in the YB<sub>66</sub> Structure

The YB<sub>66</sub> compound (RICHARDS and KASPER, 1969) is the most boron-rich phase among the metal borides thus far reported. It crystallizes in a face centered-cubic structure (space group, Fm3c) with the lattice constants a = 2.3436 nm. As shown in Fig. 27, the boron framework of  $YB_{66}$  is basically made up of the giant icosahedron unit  $B_{12}(B_{12})_{12}$  (Fig. 2) and a nonicosahedral cage. There are approximately 1584 boron atoms and 24 yttrium atoms in the unit cell. The majority of the boron atoms (1248) belong to eight  $B_{12}(B_{12})$  giant icosahedra, and the rest (336) form eight nonicosahedral cages. The giant icosahedra are located in one orientation at the face-centered cubic lattice points. They also occur at the center of the cell and cell edges rotated by 90°. The nonicosahedral cages are situated at the centers of eight octants of the cubic unit cell. In Fig. 28, the arrangement of  $B_{12}(B_{12})$  giant icosahedra on the (001) plane is projected along the c axis. In each giant icosahedron, four  $B_{12}$  icosahedra as well as the central  $B_{12}$  icosahedron are placed so as to have one of their respective mirror planes just on the (001) plane, and the remaining eight B<sub>12</sub> icosahedra are laid above and below that plane; the (001) plane is also one of the mirror planes pertaining to the space group to which this crystal belongs. The two-dimensional icosahedral  $B_{12}$ network just on the structural mirror plane is presented in Fig. 29. Unlike the icosahedral

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Fig. 27. Perspective drawing of the structure of  $YB_{66}$  (cubic, space group: Fm3c; a = 2.3436 nm). The largest circles stands for the  $B_{12}(B_{12})_{13}$  giant icosahedron, the middle ones a nonicosahedral cage, and the smallest the Y atom.



Fig. 28. The arrangement of  $B_{12}(B_{12})_{13}$  giant icosahedra in the YB<sub>66</sub> structure as seen along the <100> axes.

 $B_{12}$  networks so far described, the present network is unusual in that it consists of triangles, squares, and pentagons of  $B_{12}$  icosahedra in equal frequency. After the code of kagomé net 3636 (PEASON, 1972), this type of network might be called as "345 (or 345345)" net. The four-fold symmetry axis (pertaining to the structure) is situated at the center of each square in parallel with the <100> axes. Being forced to create pentagons, the  $B_{12}$ - $B_{12}$  bond directions are significantly deviated from the five-fold axis directions. The feature of the bent bond is more clearly seen in Fig. 30, where a section of the icosahedral  $B_{12}$  network in Fig. 29 is presented; the icosahedra at both ends of the section are those which are centered at the positions 0,0,0 and 1,0,0 in Fig. 29. It would be interesting here to compare



Fig. 29. Icosahedral B<sub>12</sub> network in the YB<sub>66</sub> structure extending on the {100} planes, showing the "345" type network.

the icosahedral  $B_{12}$  network (Fig. 29) and its section (Fig. 30) with those observed in the related compound  $YB_{41}Si_{1.2}$  (HIGASHI *et al.*, 1997). The  $YB_{41}Si_{1.2}$  compound is crystallized in the orthorhombic structure (space group, Pbam) with the lattice constants a = 1.67 nm, b = 1.767 nm, c = 0.9511 nm. It is composed of the  $B_{12}$  icosahedron and the  $B_{12}Si_{3}$  polyhedral unit. The icosahedral  $B_{12}$  network lying just on the (001) plane (which is a mirror plane of crystal structure) is presented in Fig. 31. In this network similar sections to that of  $YB_{66}$  (Fig. 30) is seen in the <110> directions, although the curved icosahedral  $B_{12}$  chains are disconnected once every translation in this direction (Fig. 32).



Fig. 30.

Fig. 31.

Fig. 30. Icosahedral  $B_{12}$  chains on the {100} planes in the YB<sub>66</sub> structure, showing a deviation of the  $B_{12}$ - $B_{12}$  linkage from the five-fold axis of the icosahedron.

Fig. 31. Icosahedral B<sub>12</sub> network in the YB<sub>41</sub>Si<sub>1.2</sub> structure extending on the (001) plane, showing disconnections of the B<sub>12</sub>-B<sub>12</sub> bonds within the "345" type network.



Fig. 32. Icosahedral B<sub>12</sub> chains on the (001) plane of the YB<sub>41</sub>Si<sub>1.2</sub> structure, showing a disconnection of the B<sub>12</sub>-B<sub>12</sub> bond every translation along the [110] direction.

#### 9. Concluding Remarks

The icosahedral  $B_{12}$  crystals can be classified into eight types according to the mode of  $B_{12}$  arrangement (HIGASHI, 1986). The two-dimensional icosahedral  $B_{12}$  networks described in the present paper are therefore related to the structures of most of icosahedral  $B_{12}$  crystals. They are all plane networks (neither wavy nor puckered) extending on or parallel to the typical crystallographic planes such as (100), (010), (001), (110), (101), and (111) planes. It is of interest to point out that most of the icosahedral networks show 3<sup>6</sup> and 3636 (kagomé) type nets (PEASON, 1972).

When the icosahedral  $B_{12}$  networks are viewed down perpendicularly, they display different features of individual icosahedral  $B_{12}$  units, depending on the structural nature of the crystal plane on which (or parallel to which) they are extending. On the (111) plane of the  $\alpha$ - or  $\beta$ -rhombohedral boron structure, the icosahedral  $B_{12}$  unit precisely shows its three-fold rotation-inversion symmetry, reflecting the same symmetry element along the [111] axis of the structures (Figs. 6, 9 and 11). (The icosahedral  $B_{12}$  network of Fig. 12 is not on the (111) plane but just in between the {111} planes.) On the other hand, the icosahedral  $B_{12}$  networks on the {100} planes of both structures show almost perfect twofold or mirror symmetry of  $B_{12}$  icosahedra (Figs. 7 and 13). In the cubic, tetragonal, and orthorhombic structures, the icosahedral  $B_{12}$  units in the icosahedral  $B_{12}$  networks display

roughly or almost exactly its two-fold or mirror symmetry (Figs. 15, 18, 19, 23, 26, 29 and 31); only one exception is seen in Fig. 22 in which the icosahedral  $B_{12}$  unit is arranged so as to have one of its five-fold axes approximately perpendicularly to the icosahedral  $B_{12}$  network. In the crystals belonging to above orthogonal crystal systems, the icosahedral  $B_{12}$ - $B_{12}$  linkages are necessarily deviated to a certain extent from the five-fold axis. This tendency is significant as for the crystals having smaller unit cell size ( $\alpha$ -tetragonal boron and AlMgB<sub>14</sub>: Figs. 16 and 24, respectively), as well as for the YB<sub>66</sub> structure in which the icosahedral B<sub>12</sub> network has the "345 (or 345345)" arrangement. As for the structure of AlB<sub>24</sub>C<sub>4</sub>, owing to the presence of C-B-C chains as a structural entity, the deviation of icosahedral B<sub>12</sub>-B<sub>12</sub> linkages is not notable in spite of its relatively small unit cell size.







Fig. 33. Average difference electron densities through (a) the triangular face and (b) the bisecting plane of the icosahedron in  $\alpha$ -AlB<sub>12</sub>.

It would be interesting to refer to the strong chemical bond within the structures of icosahedral  $B_{12}$  crystals, which is necessarily responsible for their extremely high hardness (2,000–3,000 kg/mm<sup>2</sup>) and high-melting points (higher than 2,000°C). Features of bonding electron density distributions of the  $B_{12}$  icosahedron (three-centered bond) and the  $B_{12}$ - $B_{12}$  inter-icosahedral two-centered bond are presented in Fig. 33 (ITO *et al.*, 1979). The difference electron density maps in the figure, obtained from a precision X-ray diffraction work, are reflecting the symmetry of icosaheron.

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